

29.23. Model: The charge is a point charge.

Visualize: Please refer to Figure Ex29.23.

Solve: (a) The electric potential of the point charge q is

$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{r} = (9.0 \times 10^9 \text{ N m}^2 / \text{C}^2) \left(\frac{2.0 \times 10^{-9} \text{ C}}{r} \right) = \frac{18.0 \text{ N m}^2 / \text{C}}{r}$$

For points A and B, $r = 0.01 \text{ m}$. Thus,

$$V_A = V_B = \frac{18.0 \text{ N m}^2 / \text{C}}{0.01 \text{ m}} = 1800 \frac{\text{Nm}}{\text{C}} = 1800 \left(\frac{\text{V}}{\text{m}} \right) \text{m} = 1800 \text{ V}$$

For point C, $r = 0.02 \text{ m}$ and $V_C = 900 \text{ V}$.

(b) The potential energy of a charge q' at a point where the electric potential is V is $U = q'V$. The expression for the potential in part (a) assumes that we have chosen $V = 0 \text{ V}$ to be the potential at $r = \infty$. So, we are obtaining potential/potential energy relative to a zero of potential/potential energy at infinity. Thus,

$$U_A = U_B = (q')V = (-e)(V) = -(1.60 \times 10^{-19} \text{ C})(1800 \text{ V}) = -2.88 \times 10^{-16} \text{ J}$$

$$U_C = (-1.60 \times 10^{-19} \text{ C})(900 \text{ V}) = -1.44 \times 10^{-16} \text{ J}$$

(c) The potential differences are

$$\Delta V_{AB} = V_B - V_A = 1800 \text{ V} - 1800 \text{ V} = 0 \text{ V} \quad \Delta V_{BC} = V_C - V_B = 900 \text{ V} - 1800 \text{ V} = -900 \text{ V}$$